

## IMPLEMENTATION OF CORRECTION FOR HETEROGENEOUS WITHIN HERD VARIANCES

G. de Jong, NRS, Arnhem, The Netherlands

T.H.E. Meuwissen, ID-DLO, Zeist, The Netherlands

### 1. Introduction

In April 1995 a correction for heterogeneous within herd variances was introduced in the genetic evaluation for milk production traits in The Netherlands. The applied method is described in Meuwissen et al (1994 and 1995). Results from research on this method are presented in this paper.

The goal of the research was estimation of two parameters needed for the correction for heterogeneous variances. The two parameters are the correlation between the herd\*year heterogeneity correction factors ( $\rho$ ) of adjacent years within a herd and the variance of these correction factors ( $\sigma^2$ ). Further effects on breeding values are also investigated.

### 2. Data

Milk production data from the national Dutch genetic evaluation run of April 1995 were used for this research. This data set consisted of lactation records with calving dates from July 1978 to December 1994. In total 12,629,403 lactation records of 5,819,607 cows in 42,480 herds were analysed, where 499,608 herd-year-seasons were defined.

The same animal model as used for the national genetic evaluation is used in the analysis, with the same precorrections:

$$Y_{ijklm} = HYS_i + KM_j + PERM_{kl} + A_k + \text{error}$$

where:

$Y_{ijklm}$  = 305-days lactation for milk fat and protein yield, with precorrection for:  
- age at calving  
- days open during the lactation  
- heterosis and recombination;

$HYS_i$  = herd-year-season-parity class  $i$ , in which the lactation is compared with lactations of herdmates;

$KM_j$  = calving month\*year  $j$ , when the lactation was started;

$PERM_{kl}$  = permanent environment effect  $kl$  of cow  $k$  in herd  $l$  (repeatability=.55);

$A_k$  = breeding value of cow  $k$  (heritability=.35);

error = error term of observation  $Y_{ijklm}$ .

For  $A_k$  the relation matrix is added, following the procedures of an animal model.

### 3. Results

#### 3.1 Parameters

Correlations between herd\*year heterogeneity correction factors ( $\rho$ ) for milk yield vary between 0.967 and 0.998. The highest values are found between the years at the beginning and end of the data set (table 1). The estimates for  $\rho$  approximately follow a hyperbolic function. The same results are found for fat and protein yield with the correlation for these traits also high. Fat yield varies between 0.959 and 1.00 and protein yield between 0.963 and 0.992. The average correlation between the different years is 0.984 for milk, 0.983 for fat yield and 0.980 for protein yield.

The reason for the higher  $\rho$  in the middle of the time span of the data is the influence adjacent years have on both sides of the year concerned, while the years at the side of the time span are affected mainly from one side (later or previous years).

Considering the estimated  $\rho$ , the variance lactation records of different years does not vary much from year to year.

Table 1. Correlation between the within herd herd\*year heterogeneity correction factors (rho) and the variance of these factors (vhy) per year for the traits milk, fat and protein yield.

| Year        | rho   |         |        |         | vhy   |         |        |         |
|-------------|-------|---------|--------|---------|-------|---------|--------|---------|
|             | n     | trait   |        |         | n     | trait   |        |         |
|             |       | kg milk | kg fat | kg prot |       | kg milk | kg fat | kg prot |
| oct78-sep79 | 25126 | 0.992   | 0.994  | 0.990   | 25126 | 0.107   | 0.127  | 0.147   |
| oct79-sep80 | 26253 | 0.991   | 0.994  | 0.989   | 26253 | 0.108   | 0.127  | 0.147   |
| oct80-sep81 | 26804 | 0.990   | 0.993  | 0.985   | 27228 | 0.108   | 0.123  | 0.144   |
| oct81-sep82 | 27404 | 0.988   | 0.991  | 0.982   | 27734 | 0.105   | 0.117  | 0.139   |
| oct82-sep83 | 28040 | 0.984   | 0.985  | 0.978   | 28409 | 0.102   | 0.110  | 0.134   |
| oct83-sep84 | 28348 | 0.977   | 0.973  | 0.972   | 28998 | 0.100   | 0.103  | 0.129   |
| oct84-sep85 | 28564 | 0.974   | 0.967  | 0.969   | 29148 | 0.095   | 0.094  | 0.123   |
| oct85-sep86 | 28373 | 0.967   | 0.959  | 0.963   | 29268 | 0.092   | 0.088  | 0.120   |
| oct86-sep87 | 27599 | 0.970   | 0.963  | 0.966   | 28806 | 0.091   | 0.085  | 0.118   |
| oct87-sep88 | 26913 | 0.976   | 0.973  | 0.972   | 27956 | 0.092   | 0.086  | 0.120   |
| oct88-sep89 | 26401 | 0.982   | 0.980  | 0.977   | 27211 | 0.095   | 0.089  | 0.123   |
| oct89-sep90 | 25851 | 0.985   | 0.984  | 0.981   | 26642 | 0.099   | 0.094  | 0.129   |
| oct90-sep91 | 25017 | 0.991   | 0.992  | 0.986   | 26025 | 0.104   | 0.099  | 0.136   |
| oct91-sep92 | 24273 | 0.992   | 0.992  | 0.987   | 25235 | 0.110   | 0.105  | 0.143   |
| oct92-sep93 | 23529 | 0.994   | 0.995  | 0.992   | 24406 | 0.114   | 0.109  | 0.149   |
| oct93-sep94 | 20179 | 0.998   | 1.003  | 0.989   | 23529 | 0.114   | 0.108  | 0.149   |
| oct94-sep95 |       | -       | -      | -       | 20179 | 0.112   | 0.104  | 0.141   |
| average     |       | 0.984   | 0.983  | 0.980   |       | 0.103   | 0.104  | 0.135   |

The variance of herd\*year heterogeneity correction factors (vhy) varies between 0.091 and 0.114 for milk yield, with an average of 0.103 (table 1). The lowest estimates are found for the years in the middle of the time span of the data set. For fat yield the vhy varies between 0.085 and 0.127, with an average of 0.104. The estimates for protein yield are higher: varying between 0.118 and 0.149, with an average of 0.135.

### 3.2 Breeding values

A test to check how the correction method works is to compare parent average (PA) of progeny tested bulls with the realized breeding value (RBV) of these bulls. When comparing the results of no correction for heterogeneity and applying the correction method (table 2), it is obvious that the average PA is higher than the average realized breeding value. The difference between average PA and average realized breeding value is smaller (25%) with correction than without correction. The genetic trend in breeding values for tested bulls is similar for both methods, 1049 kg milk without correction and 1086 kg milk with correction, in 10 years (table 3). The same is found for the trend in PA with 1119 kg milk without correction and 1111 kg milk with correction, in 10 years. Taking a closer look where differences between PA and RBV start for both methods (table 2), it can be seen that dams of bulls especially cause differences between PA and RBV (table 3). The dams' breeding values appear to be overestimated values while sires

Table 2. Realized breeding values minus parent average for progeny tested bulls per year of birth.

| Year of birth | Number | Without correction | With correction |
|---------------|--------|--------------------|-----------------|
| 81            | 87     | -97                | -89 ( 8%)       |
| 82            | 139    | -158               | -143 ( 8%)      |
| 83            | 153    | -106               | -82 (23%)       |
| 84            | 226    | -152               | -123 (19%)      |
| 85            | 206    | -104               | -80 (23%)       |
| 86            | 200    | -190               | -159 (16%)      |
| 87            | 167    | -150               | -94 (37%)       |
| 88            | 158    | -215               | -160 (26%)      |
| 89            | 105    | -181               | -130 (28%)      |
| 90            | 78     | -167               | -114 (32%)      |

\*(Bulls have at least 75% HF genes and their dams realized a lactation in The Netherlands. The base for the correction for heterogeneous variances is the average correction factor for cows born in 1990.)

of bulls do not show differences for both methods. On average dams are estimated 60 to 80 kg milk higher without correction for heterogeneity than with this correction.

The average breeding value of The Netherlands progeny tested bulls (having a first crop of daughters) are 20 kg milk higher with correction than without correction (table 4). Imported bulls (with second crop daughters) received, on average, a 20 kg lower breeding value for milk yield with correction compared to without correction. The absolute differences (about 55 kg milk) and standard deviation of differences (about 70 kg milk) are higher for imported bulls than for progeny tested bulls. Progeny tested bulls showed an absolute difference of breeding values of 30 kg milk and a standard deviation of 30 kg milk for both methods. The changes for imported bulls were twice as large than for progeny tested bulls, although differences were relatively small.

Table 3. Realized breeding values(RBV), parent average(PA) and breeding values for sires and dams for progeny tested bulls per year of birth.

| Year of birth | Number | Without correction |      |      |      | With correction |      |      |      |
|---------------|--------|--------------------|------|------|------|-----------------|------|------|------|
|               |        | RBV                | PA   | dam  | sire | BV              | PA   | dam  | sire |
| 81            | 87     | -596               | -499 | -734 | -263 | -618            | -529 | -813 | -246 |
| 82            | 139    | -565               | -408 | -667 | -148 | -583            | -440 | -749 | -131 |
| 83            | 153    | -371               | -265 | -593 | 64   | -372            | -290 | -656 | 76   |
| 84            | 226    | -329               | -177 | -513 | 160  | -323            | -199 | -572 | 174  |
| 85            | 206    | -278               | -174 | -482 | 134  | -271            | -191 | -535 | 154  |
| 86            | 200    | -183               | 8    | -249 | 264  | -168            | -9   | -302 | 285  |
| 87            | 167    | 100                | 250  | 23   | 478  | 123             | 217  | -39  | 474  |
| 88            | 158    | 145                | 359  | 194  | 5225 | 167             | 327  | 131  | 522  |
| 89            | 105    | 251                | 431  | 313  | 550  | 270             | 400  | 240  | 559  |
| 90            | 78     | 453                | 620  | 548  | 693  | 468             | 582  | 477  | 686  |
| 81-90         |        | 1049               | 1119 |      |      | 1086            | 1111 |      |      |

\*(Bulls have at least 75% HF genes and their dams realized a lactation in The Netherlands. The base for the correction for heterogeneous variances is the average correction factor for cows born in 1990.)

More changes in breeding values are also found with imported bulls than with progeny tested bulls for fat yield and protein yield (for protein see table 5). The standard deviation of differences for protein yield was 2.2 kg, twice the standard deviation found for progeny tested bulls (1.1 kg protein). The larger differences of breeding values for imported bulls may be caused by the kind of herd their daughters are producing in. The average production level of herds using imported semen is higher than the average herd production level. As it is known that with the increase of production level, the variation of lactations also increases, it is logical that imported bulls are affected more by the correction method than progeny tested bulls.

Table 4. Comparison of breeding values for milk yield for progeny tested bulls and imported bulls.

| Progeny tested bulls |           |              |            |          |     | Imported bulls |           |              |            |          |    |
|----------------------|-----------|--------------|------------|----------|-----|----------------|-----------|--------------|------------|----------|----|
| year of birth        | avg. diff | avg abs diff | stand dev. | max diff | n   | year of birth  | avg. diff | avg abs diff | stand dev. | max diff | n  |
| 85                   | 19.3      | 29           | 29.9       | 179      | 371 | 81             | -12.8     | 54.6         | 74.5       | 202      | 73 |
| 86                   | 22.1      | 30           | 30.2       | 153      | 333 | 82             | -12.0     | 48.9         | 70.0       | 249      | 82 |
| 87                   | 24.6      | 33           | 34.1       | 183      | 323 | 83             | -20.9     | 55.7         | 68.0       | 248      | 61 |
| 88                   | 23.1      | 32           | 31.0       | 114      | 384 | 84             | -16.4     | 58.2         | 76.6       | 244      | 45 |
| 89                   | 19.8      | 31           | 34.4       | 157      | 412 | 85             | -18.8     | 56.0         | 72.1       | 221      | 44 |
| 90                   | 18.2      | 27           | 27.9       | 88       | 290 | 86             | -24.3     | 55.6         | 78.4       | 283      | 53 |

\*(The difference (diff) is calculated as breeding value with heterogeneous variance correction minus without this correction).

Table 5. Comparison of breeding values for protein yield for progeny tested bulls and imported bulls.

| Progeny tested bulls |           |              |            |          |     | Imported bulls |           |              |            |          |    |
|----------------------|-----------|--------------|------------|----------|-----|----------------|-----------|--------------|------------|----------|----|
| year of birth        | avg. diff | avg abs diff | stand dev. | max diff | n   | year of birth  | avg. diff | avg abs diff | stand dev. | max diff | n  |
| 85                   | 0.6       | 1.0          | 1.0        | 3        | 371 | 81             | 0.2       | 1.7          | 2.0        | 5        | 73 |
| 86                   | 0.8       | 1.0          | 1.1        | 5        | 333 | 82             | 0.0       | 1.4          | 2.0        | 6        | 82 |
| 87                   | 0.7       | 1.0          | 1.1        | 5        | 323 | 83             | 0.0       | 1.6          | 2.2        | 6        | 61 |
| 88                   | 0.7       | 1.0          | 1.1        | 4        | 384 | 84             | 0.0       | 1.4          | 1.8        | 4        | 45 |
| 89                   | 0.6       | 1.0          | 1.2        | 5        | 412 | 85             | 0.1       | 1.6          | 2.1        | 5        | 44 |
| 90                   | 0.6       | 0.9          | 1.1        | 4        | 290 | 86             | -0.1      | 1.6          | 2.3        | 9        | 53 |

\*(The difference (diff) is calculated as breeding value with heterogeneous variance correction minus without this correction)

## Literature

Meuwissen, T.H.E., G. de Jong en B. Engel, 1994. Joint estimation of breeding values and heterogeneous variances by mixed model equations in large national data sets. Proceedings of the open session of Interbull meeting Ottawa Canada, 1994, Interbull Bulletin no 10.

Meuwissen, T.H.E., G. de Jong en B. Engel, 1995. Joint estimation of breeding values and heterogeneous variances in large scale dairy data. Submitted.